5. [13 points] Roo is a boxing kangaroo in Australia. Every Sunday, Roo has a boxing match against a professional boxer at the Sydney Opera House.

Let $r(t)$ be the revenue, in dollars, that the opera house makes from ticket sales when it sells $t$ tickets to one of Roo's matches. Then

$$
r(t)=t\left(230-\frac{1}{30} t\right)
$$

Note: The capacity of the Sydney Opera House is 5738 , so there are never more than 5738 tickets sold to a match.
a. [5 points] If the opera house had a revenue of $\$ 159,120$ from ticket sales to last week's match, how many tickets did they sell? Remember to show your work carefully.

## Answer:

$\qquad$
b. [6 points] Use the method of completing the square to put the formula for $r(t)$ in vertex form. Carefully show your algebraic work step-by-step.

Answer: $r(t)=$ $\qquad$
c. [2 points]

What is the maximum possible revenue? $\qquad$

How many tickets are sold to make the maximum possible revenue? $\qquad$

