

8. [14 points] An ice cube is left to melt in a warm room. Let $V = f(t)$ be the volume of the ice cube (in cm^3) t seconds after it starts melting. Also, as the ice cube melts, a circular puddle of water of radius r (in cm) and area A (in cm^2) starts forming around it. Let g and h be functions such that $r = g(t)$ and $A = h(r)$. You may assume f , g and h are invertible.

- a. [6 points] Select a mathematical expression from the list below that represents each of the following statements.

- (i) When the volume of the ice cube is 30 cm^3 , the radius of the water puddle around the ice cube is 6 cm.

Answer: _____

- (ii) The radius of the water puddle grows by 6 cm between 20 and 30 seconds after the ice cube started melting.

Answer: _____

- (iii) Between 20 and 30 seconds after the ice cube started melting, the radius of the water puddle grows, on average, by 6 cm per second.

Answer: _____

A) $f(g(6)) = 30$

B) $\frac{g(30) - g(20)}{10} = 6$

C) $g(30) = 6$

D) $\frac{g(30) - g(20)}{20} = 6$

E) $f(g^{-1}(6)) = 30$

F) $\frac{g(30) + g(20)}{2} = 6$

G) $g(30) - g(20) = 6$

H) $f(6) = 30$

J) $g(20) - g(30) = 6$

- b. [4 points] The following statements are practical interpretations of mathematical expressions (not necessarily the ones listed above). Write the mathematical expression in each case.

- (i) The time (in seconds) it takes for the radius of the water puddle around the ice cube to be 7 cm.

Answer: _____

- (ii) The area (in cm^2) of the circular water puddle formed around the ice cube 9 seconds after the ice cube started melting.

Answer: _____

- c. [4 points] Assume that the domains of f and g is the interval of time it takes for the entire ice cube to melt. Indicate if the following functions are increasing, decreasing or neither.

$f(t)$ _____

$h(g(t))$ _____