

7. [17 points] Passengers on a cruise ship watch as nearby dolphins and porpoises jump through the waves. When one dolphin jumps, its height above the water (measured in feet)  $t$  seconds after leaving the water is given by  $w(t) = -16t^2 + 96Dt$  for some positive constant  $D$ .
- a. [3 points] After how many seconds, in terms of  $D$ , does this dolphin land back in the water?

**Answer:** \_\_\_\_\_

- b. [7 points] Use the method of completing the square to rewrite  $w(t)$  in vertex form. What is the vertex of the graph of  $w(t)$ ? (Carefully show your work step-by-step. Your answers may involve  $D$ .)

**Vertex Form:**  $w(t) =$  \_\_\_\_\_ **Vertex:** \_\_\_\_\_

- c. [2 points] If the dolphin reaches a maximum height of 16 ft before falling back to the water, find the value of  $D$ .

**Answer:**  $D =$  \_\_\_\_\_

- d. [5 points] A nearby porpoise is also seen jumping. Its height above the surface of the water (measured in meters)  $t$  seconds after the *dolphin* left the water is given by  $h(t) = -5t^2 + 24t - 26$ . For how long is the porpoise above the surface of the water? *Solve for the answer algebraically and give your final answer either in exact form or accurate to at least three decimal places.*

**Answer:** \_\_\_\_\_