

1. [14 points] Figure 1 below gives some data for an invertible function  $f(x)$  and Figure 2 shows the graph of a function  $g(x)$ . Use this information to answer the questions below.

$x$	0	1	2	3	4	5	6
$f(x)$	1	5	8	9	7	4	0

Figure 1

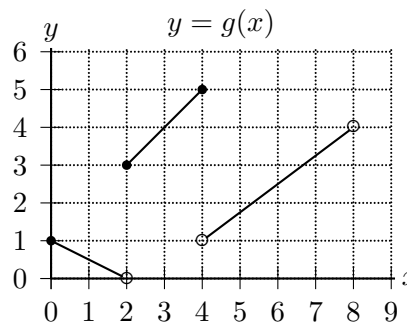


Figure 2

- a. [4 points]

- i. Evaluate  $2g(2)$ .

*Solution:* From the graph, we see that  $g(2) = 3$ .  
So  $2g(2) = 2(3) = 6$ .

**Answer:** 6

- ii. Evaluate  $f^{-1}(5)$ .

*Solution:* From the table, we see that  $f(1) = 5$ . So  $f^{-1}(5) = 1$ .

**Answer:** 1

- iii. Evaluate  $f(f(1))$ .

*Solution:* From the table, we see that  $f(1) = 5$ .  
So  $f(f(1)) = f(5) = 4$ .

**Answer:** 4

- iv. Solve  $f(x) = g(3)$  for  $x$ .

*Solution:* From the graph we see that  $g(3) = 4$ . So we are to solve  $f(x) = 4$ . From the table, we see that the solution is  $x = 5$ .

**Answer:**  $x = 5$

- b. [3 points] Which of the following numbers are in the *range* of  $g$ ?  
(Circle ALL correct answers.)

0     1     1.5      $\pi$      4     5    5.25    7    8    9

- c. [7 points] Find a formula for  $g(x)$  as a piecewise-defined function.

*Solution:* The first piece appears to be linear with slope  $-0.5$  and vertical intercept 1 so on this piece,  $g(x) = 1 - 0.5x$ . The second piece appears to be linear with slope 1 and vertical intercept 1, so on this piece,  $g(x) = 1 + x$ . The third piece appears to be linear with slope  $3/4$ , so using the point  $(4, 1)$  and point-slope form, a formula for this piece is  $g(x) = 1 + 0.75(x - 4) = -2 + 0.75x$ . Hence a formula for  $g(x)$  is

$$g(x) = \begin{cases} 1 - 0.5x & \text{if } 0 \leq x < 2 \\ 1 + x & \text{if } 2 \leq x \leq 4 \\ -2 + 0.75x & \text{if } 4 < x < 8 \end{cases}$$