3. [11 points] At 8:00 am, a water pump is turned on and water starts filling a swimming pool. Consider the following functions:

a) Let $F(t)$ be the number of gallons of water the pump has put into the swimming pool $t$ minutes after 8 am.

b) Let $G(x)$ be the depth of the water in the swimming pool, in inches, when it contains $x$ gallons of water.

Assume that all the functions defined above are invertible.

a. [6 points] Give a practical interpretation to the following mathematical expressions:

i) $G^{-1}(30)$:

ii) $G(F(30))$:

b. [5 points]

i) Let $D$ be the number of gallons of water the pump puts into the swimming pool between 8:15 am and 8:30 am. Find a mathematical expression for the constant $D$ in terms of any of the functions defined above.

\[ D = \quad \]

ii) Let $H(m)$ be the amount of water, in gallons, put by the water pump in the swimming pool $m$ minutes after 9:00 am. Find a formula for $H(m)$ in terms of any of the functions defined above.

\[ H(m) = \quad \]