

3. [8 points] Jaime is on a long car trip. Consider the following functions:

- Let $d(t)$ be the distance, in miles, Jaime has driven t minutes after they begin their trip.
- Let $g(t)$ be the amount of gas, in gallons, in Jaime's car's gas tank t minutes after they begin their trip.

Assume that both functions have inverses. For each part below, write a phrase or sentence giving a practical interpretation of the given expression or equation, or explain why it doesn't make sense in this context.

a. $d(9) = 4$

Solution: When Jaime has driven for 9 minutes, they've gone 4 miles.

b. $g(d^{-1}(120))$

Solution: the amount of gas, in gallons, in Jaime's car's tank when they've driven 120 miles

c. $g(60) = g(0) - 2$

Solution: 60 minutes into their trip, Jaime's car has 2 fewer gallons of gas than when their trip started.

4. [15 points] Mei is starting a coffee roasting business.

- a. [4 points] Mei puts green coffee beans into her roaster. Let $T(t)$ be the temperature, in degrees Fahrenheit ($^{\circ}\text{F}$), inside the roaster t minutes after she starts roasting the beans. Some values of $T(t)$ are given in the table below.

t	0	3	5	12
$T(t)$	70	370	470	320

Compute the average rate of change of $T(t)$ over the interval $[0, 5]$. **Include units.**

Solution: $\frac{470 - 70}{5 - 0} = \frac{400}{5} = 80$

Answer: 80 $^{\circ}\text{F}$ per minute

Could $T(t)$ be concave down on the entire interval $[0, 12]$? Show your work, and circle your final answer.

Solution: The average rates of change over the three consecutive subintervals are $\frac{370 - 70}{3 - 0} = 100$, $\frac{470 - 370}{5 - 3} = 50$, and $\frac{320 - 470}{12 - 5} < 0$. Since these are decreasing, yes, the function could be concave down on this interval.

Answer (circle one): **Yes** **No**

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