6. [6 points] A sculpture of a star of height S (measured in meters) is mounted on a base of height B(measured in meters). Reina is standing at a distance of 10 meters away from the base of the statue, at the point R.



The measures of the angles LRM and LRP are  $42^{\circ}$  and  $62^{\circ}$  respectively. Note that the diagram above is not drawn to scale. For this problem, you should show your work, and write your answers in the spaces provided.

**a.** [3 points] Write an expression for the height S of the star. Your answer may involve the constant B.

**Solution**: Since LPR is a right angle, we have:  $\tan(62^\circ) = \frac{S+B}{10}$ 

and solving for 
$$S$$
 gives us:

$$S = 10\tan(62^\circ) - B$$

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**b**. [3 points] Find the height B of the base of the statue. Your answer for this part **cannot** involve S.

**Solution:** Since MPR is a right angle and the measure of angle MRP is  $62^{\circ} - 42^{\circ} = 20^{\circ}$ , we have: В t,

$$\operatorname{an}(20^\circ) = \frac{D}{10}$$

 $B = 10\tan(20^\circ)$ 

and solving for B gives us:

$$B = 10\tan(20^\circ)$$