8. [8 points] Chuck had a strange yet familiar dream on the night he got back to the farm. His path was blocked by a fast-flowing river. Spying a small tree beside the river, Chuck thought about cutting down the tree to make a log bridge. He knows the points $A$ and $B$ are three meters apart, and he knows the angle between the ground and the line from the points $A$ and $B$ to the top of the tree. The tree is $h$ meters tall and makes a right angle with the ground. The figure below depicts the situation.


Please leave your answers in exact form.
a. [4 points] Write expressions for $\tan \left(40^{\circ}\right)$ and $\tan \left(50^{\circ}\right)$ in terms of $d$ and $h$.

$$
\begin{aligned}
& \tan \left(40^{\circ}\right)= \\
& \tan \left(50^{\circ}\right)=
\end{aligned}
$$

b. [4 points] Solve the system of equations you got in part (a) to find $h$ in terms of $\tan \left(40^{\circ}\right)$ and $\tan \left(50^{\circ}\right)$ (and not in terms of $d$ ).

$$
h=
$$

$\qquad$

