

5. [10 points] The temperature  $T$  in a given room, measured in  $^{\circ}\text{F}$ , after an air conditioner is turned on is given by  $T = f(t) = 68 + 5e^{-0.02t}$ , where  $t$  is measured in minutes.

a. [4 points] Find the following limits of  $f(t)$ :

(i)  $\lim_{t \rightarrow \infty} f(t) = \underline{\hspace{2cm}}$

(ii)  $\lim_{t \rightarrow -\infty} f(t) = \underline{\hspace{2cm}}$

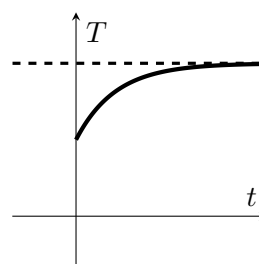
b. [3 points] Find a formula for  $t = f^{-1}(T)$ .

$$f^{-1}(T) = \underline{\hspace{4cm}}$$

c. [3 points]

The graph of  $T = q(t)$  to the right shows the temperature in a different room when being *heated* as a function of time  $t$ . The domain shown is  $[0, \infty)$  and the dashed line represents a horizontal asymptote of  $q(t)$ .

Given that behavior, which of the following *could* be a formula for  $q(t)$ ? (*Circle all that apply.*)



$$q(t) = 3 \log(t + 2)$$

$$q(t) = 50 \cdot 1.02^t$$

$$q(t) = -0.7^t + 65$$

$$q(t) = -3 \log(t + 5)$$

$$q(t) = -e^{-0.2t} + 67$$

$$q(t) = -e^{0.1t} + 69$$