

5. [10 points]

a. [2 points] Consider the function  $P(t)$  defined by

$$P(t) = \begin{cases} \frac{70t(t-6)}{(t-10)(t+2)} & \text{if } 0 \leq t \leq 5 \\ 2 + 5e^{5-t} & \text{if } t > 5. \end{cases}$$

Evaluate  $P(5)$  and  $P(P(5))$ .

$$P(5) = \underline{\hspace{4cm}} \qquad P(P(5)) = \underline{\hspace{4cm}}$$

b. [4 points] Below, you are given a table with some data about two functions:  $f(t)$  and  $h(t)$ . You are also given information about some transformations and combinations of these functions. Fill in the missing entries in the table. You may assume  $f(t)$  and  $h(t)$  are invertible functions. *No work or explanation is required.*

|             |    |    |   |    |
|-------------|----|----|---|----|
| $t$         | 0  | 1  | 2 | 3  |
| $f(t)$      | 2  | 4  | 5 | 9  |
| $h(t)$      | 3  | 8  |   | 7  |
| $f(h(t))$   |    | 6  | 4 | 11 |
| $f^{-1}(t)$ | 12 | 11 |   | 10 |
| $f(t+3)$    |    | 7  | 8 | 12 |

c. [4 points] Suppose  $g(x)$  is a power function such that  $g(1) = 3$  and  $g(5) = 6$ . Find a formula for  $g(x)$  in terms of  $x$ . *Give your answer in exact form.*

$$g(x) = \underline{\hspace{4cm}}$$