

4. [8 points] The number of people  $p$  (in thousands) who are sick with the flu virus  $t$  days after January 1, 2014 is given by

$$p = g(t) = \frac{3}{1 + e^{-0.3t}}$$

- a. [4 points] Find a formula for  $g^{-1}(p)$ . Show all your steps to receive full credit.

$$g^{-1}(p) = \underline{\hspace{4cm}}$$

- b. [2 points] What is a practical interpretation of  $g^{-1}(2)$ ? You do not need to compute its value. Include units.

- c. [2 points] The quantity of flu vaccine  $q$  (in liters) produced by a company  $t$  days after January 1, 2014 is given by

$$q = f(t) = \frac{\sqrt{5} t^2}{(1 + 2t)^2}.$$

What eventually happens to the quantity of flu vaccine produced? Give your answer in **exact form**.

$$\lim_{t \rightarrow \infty} f(t) = \underline{\hspace{4cm}}$$