**1.** [11 points] Pam the Plumber charges customers P(t) dollars for a t hour visit to their house. A graph of C = P(t) is shown below.



**a**. [2 points] Find the value of P(0) and explain what it means in context.

P(0) = 100

Meaning: This is how much Pam charges to arrive at house, without having done any work yet.

**b**. [2 points] Find the slope of P(t) and explain what it means in context.

Slope: 100/3

Meaning: After her arrival cost, for every 3 hours Pam stays, she charges \$100. Or, she charges \$33.34 / hour.

c. [2 points] Beth the Bathtub-fixer charges \$50 for a home visit plus \$40/hour spent there. Let B(t) be the amount she charges for a t hour visit. Add the graph of C = B(t) for  $0 \le t \le 8$  to axes above. Clearly label at least two points on your graph with their (t, C) coordinates.

Solution: See graph above.

d. [5 points] Find the coordinates of the point where the two graphs intersect and explain what this means in context. Show all work. Give your final answer in exact form, or rounded to at least two decimal places.

Solution: We need to find where the two linear equations intersect. To do this we can solve the following equation for t:

$$50 + 40t = 100 + 100t/3$$

By adding and subtracting terms from both sides, this simplifies to:

$$20t/3 = 50$$

which finally is equivalent to:

$$t = 150/20 = 7.5$$

To find the C-coordinate, we can plug t = 7.5 into either expression. In particular:

$$50 + 40 \times 7.5 = 350$$

**Point** (t, C) = (7.5, 350)

Meaning: This means that when Pam and Beth each work 7.5 hours, they earn the same amount of money for the visit.