4. [12 points]
a. [4 points] The graph of a polynomial $p(x)$ is shown below. The following facts are known about $p(x)$ :
i) The only zeros of $p(x)$ are $x=-2$ and $x=3$.
ii) The degree of $p(x)$ is at most four.
iii) The point $(1,9)$ is on the graph of $p(x)$.

Find a formula for $p(x)$.


$$
p(x)=
$$

$\qquad$
b. [5 points] Let

$$
R(x)=\frac{\left(x^{2}+9\right)(10 x+1)}{7 x^{3}-x}
$$

Find all the intercepts and all horizontal and vertical asymptotes of the graph $y=R(x)$. If appropriate, write "None" in the answer blank provided. Your answers should be in exact form.
i) $x$-intercept(s): $\qquad$
ii) $y$-intercept(s): $\qquad$
iii) vertical asymptote(s): $\qquad$
iv) horizontal asymptote(s): $\qquad$
c. [3 points] A law of physics states that the force $F$ (in Newtons) exerted between two objects is inversely proportional to the square of the distance $r$ (in meters) between them, and $F=30$ when $r=7$. Find a formula for $F$ in terms of $r$.

$$
F(r)=
$$

$\qquad$

