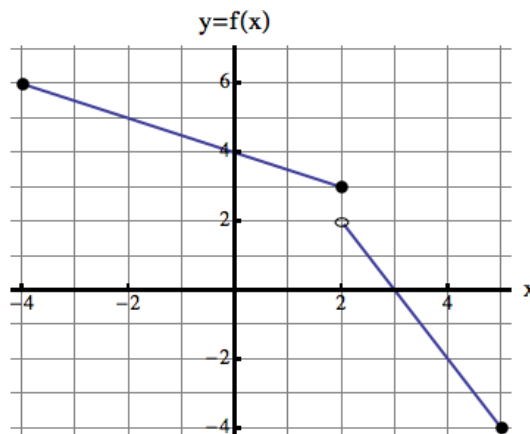


1. [13 points] Consider the functions $f(x)$ and $g(x)$, where $g(x) = 2 - \frac{1}{2}x$ and the graph of $y = f(x)$ is shown below.



- a. [9 points]

- i) Compute the value of the following expressions. Write "Undefined" if the value of the expression is not defined or there is not enough information to be computed.

$$\text{Solution: } 2f(-2) + 3f(4) = 2(5) + 3(-2) = 4 \qquad f^{-1}(3) = 2$$

$$f(g(2)) = f(2 - 0.5(2)) = f(1) = 3.5 \qquad g(g^{-1}(5)) = 5$$

- ii) Find the horizontal and vertical intercepts of the function $y = f(g(x))$.

Solution:

Horizontal intercept: If $f(g(x)) = 0$ then $g(x) = 3$. Hence $2 - \frac{1}{2}x = 3$ then $x = -2$. Hence the horizontal intercept is at **(-2,0)**.

Vertical intercept: $y = f(g(0)) = f(2) = 3$. Hence the vertical intercept is at **(0,3)**.

- iii) Find the average rate of change of $f(x)$ between $x = 2$ and $x = 5$. Show your work.

$$\text{Solution: } \text{Average rate of change of } f(x) = \frac{f(5) - f(2)}{5 - 2} = \frac{-4 - 3}{3} = -\frac{7}{3}.$$

- b. [4 points] Find a piecewise defined formula for $f(x)$.

Solution:

$$f(x) = \begin{cases} 4 - \frac{1}{2}x & -4 \leq x \leq 2 \\ -2x + 6 & 2 < x \leq 5 \end{cases}$$