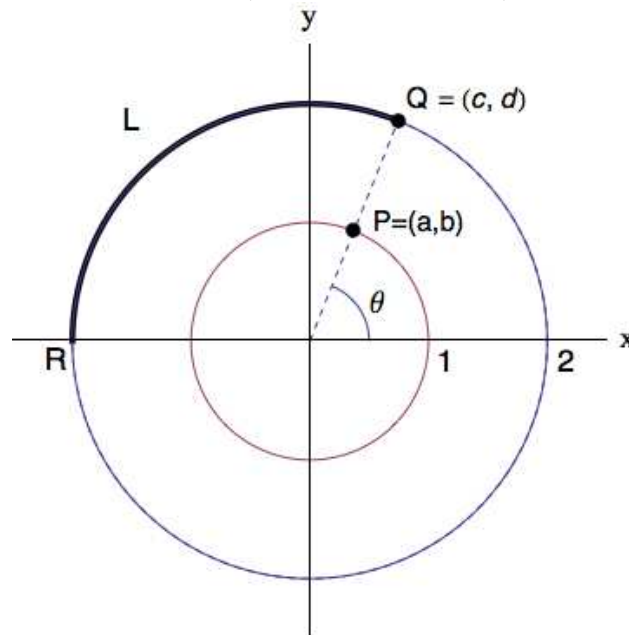


6. [6 points] The points  $P = (a, b)$  and  $Q = (c, d)$  lie on the unit circle and the circle of radius 2, respectively, centered at the origin. The point  $P$  lies in the line segment between the origin and the point  $Q$ . The angle  $\theta$  (measured in radians), is formed by the positive  $x$ -axis and the line between the origin and the point  $Q$  (see the figure below).



- a. [2 points] Find an expression in terms of  $\theta$  that computes the length  $L$  of the arc between the points  $Q$  and  $R = (-2, 0)$  (see the the arc in bold in the figure above).

$$L = \underline{\hspace{2cm}}$$

$$\boxed{\text{Solution: } L = 2(\pi - \theta).$$

- b. [4 points] Find a formula for each of the quantities below **only** in terms of the constants **a** and/or **b**.

$$\cos \theta = \underline{\hspace{2cm}}$$

$$\tan \theta = \underline{\hspace{2cm}}$$

$$c = \underline{\hspace{2cm}}$$

$$\sin(\theta + \pi) = \underline{\hspace{2cm}}$$

$$\boxed{\text{Solution: } \cos \theta = a \quad \tan \theta = \frac{b}{a} \quad c = 2a \quad \sin(\theta + \phi) = -b.$$