

5. [15 points] Consider the functions $f(x)$, $g(x)$ and $j(x)$ given by the tables below

| | | | | |
|--------|------|-----|-----|-----|
| x | -1 | 1 | 3 | 5 |
| $f(x)$ | 11.1 | 6.5 | 4.1 | 3 |
| $g(x)$ | 2.4 | 1.7 | 1 | 0.3 |
| $j(x)$ | 0.25 | 0.5 | 1 | 2 |

Assume that all the functions above are invertible.

- a. [2 points] Which function(s) could be concave up? Circle all possible answers.

$f(x)$ $g(x)$ $j(x)$ None of these

- b. [2 points] Which function(s) could be a linear function? Circle all possible answers.

$f(x)$ $g(x)$ $j(x)$ None of these

- c. [2 points] Which function(s) could be an exponential function? Circle all possible answers.

$f(x)$ $g(x)$ $j(x)$ None of these

- d. [4 points] Compute the value of the following quantities. If there is not enough information to compute the values write "Undefined".

$$g(f^{-1}(3)) = \underline{\hspace{2cm}} \qquad (j(g(3)))^{-1} = \underline{\hspace{2cm}}$$

- e. [3 points] Let $Q(t) = 3t^2 + 1$ and h be a constant. Find a simplified formula for $\frac{Q(t+h) - Q(t)}{h}$. Your answer may depend on t and h .

Answer = $\underline{\hspace{2cm}}$

- f. [2 points] Let $H(x) = \cos(1 + 2 \log(x))$ and $G(x) = \log(x)$. Find a function $F(x)$ such that $H(x) = F(G(x))$.

$$F(x) = \underline{\hspace{2cm}}$$