

2. [11 points]

- a. [2 points] Let  $f(x) = \frac{3x^2}{10x^2 + x + 1} + 5$ . Find the equation of the horizontal asymptote of the graph of  $f(x)$ . If the graph has no horizontal asymptote, write "None".

Horizontal asymptote: \_\_\_\_\_.

- b. [2 points] For which of the following values of  $x$  is the function  $f(x) = \sin(x)$  invertible? Circle all that apply.

$$\frac{\pi}{2} \leq x \leq \frac{3\pi}{2} \quad 0 \leq x \leq \pi \quad -\frac{\pi}{2} \leq x \leq \frac{\pi}{2} \quad 0 \leq x \leq 2\pi \quad \text{None of these.}$$

- c. [3 points] Find the equations of the vertical asymptotes and the  $x$  coordinate(s) of the

hole(s) of the function  $f(x) = \frac{(x-2)(x-3)}{2x^2 - 5x + 2}$ .

Write "None" if the graph of this function does not have a hole or a vertical asymptote. Show all your work.

Vertical asymptotes: \_\_\_\_\_ Holes: \_\_\_\_\_.

- d. [4 points] Fill in the blanks:

i) Let  $r(x) = (x^4 - 5)^4$ . If with  $r(x) = H(G(x))$  with  $H(x) = x^4$ , then

$$G(x) = \underline{\hspace{2cm}}$$

ii) Let  $k(x) = 2e^{2x+1}$ . If  $k(x) = F(2x)$  then  $F(x) = \underline{\hspace{2cm}}$ .