(8 points) (a) Find a value of k so that the function

$$f(x) = \begin{cases} 1-x, & \text{if } x < 3; \\ kx-4k, & \text{if } x \geq 3. \end{cases}$$

is continuous on every interval.

both functions are linear. We need them to meet at x=3. Thus, 1-3= k(3)-4k -> -2=-k, so (k=2)

(b) Is the function you found differentiable at x = 3? Explain why or why not

as x=3, the stop of + is -1, but as x > 3t, +6 stops is 2 (since for 223, fa)=26-8) Those is a sharp comes @ x= 3. Thus, f is not differentiable of x=3. There is a corner in the graph 6. (12 points) Are the given statements true or false? Give an explanation for each answer.

(a) If the graph of a function q is obtained by shifting the graph of a function f vertically upward by 3 units, then g' = f' + 3.

Jula. of 365= f(x)+3, Hen 36)-f(x). a vertical shift does not clarg the step of.

(b) If a function is not differentiable then it is not continuous

at x=0 but not differentiable there.

(c) If f" > 0, then f is increasing.

July. In Mande, y-exis decreasing, but f">0.

(d) The inequality $\sqrt{x} < 2\log(x^4)$ holds for large positive values of x (that is, as $x \to +\infty$).

Jako. as x - 20 Tx (n any Bositiv Come University of Michigan Department Mathematical Bound 3x ...). Fall, 2002 Math 115 Exam 1 Problem