

2. Suppose $A(t)$ is a function that gives the average high temperature (in $^{\circ}F$) in Ann Arbor as a function of t measured in months where $t = 0$ represents January (the coldest month in Ann Arbor).

- (a) (2 points) Puerto Montt, a city in Chile, is approximately the same distance from the equator as Ann Arbor, but it is in the southern hemisphere where the warmest month is January. Let $P(t)$ be a function that gives the average high temperature in $^{\circ}F$ in Puerto Montt as a function of time, t , in months. Write $P(t)$ in terms of $A(t)$.

$$P(t) = A(t - 6) \text{ or, (equally acceptable) } P(t) = A(t + 6)$$

- (b) (2 points) The average high temperatures in Montreal are approximately $10^{\circ}F$ less than the average highs in Ann Arbor. If $M(t)$ is a function that gives the average high temperature in Montreal as a function of time, t in months, express $M(t)$ in terms of $A(t)$.

$$M(t) = A(t) - 10$$

- (c) (5 points) The average high temperature in Ann Arbor ranges from a low of $30^{\circ}F$ in January to a high of $84^{\circ}F$ in July. Use this information to write $A(t)$ as trigonometric function.

$$A(t) = -27 \cos\left(\frac{\pi}{6}t\right) + 57$$

- (d) (1 point) What is the amplitude of the function found in (c)? 27

- (2 points) What is the period of the function found in (c)? 12 months