

5. [10 points] Electric cars need large amounts of energy to operate. Most types of batteries, including those found in electric cars, have reduced capacities when discharged at higher rates. For the lithium-ion batteries used in the newest electric cars, this relationship can be expressed by the equation  $C = f(I) = \frac{K}{I^n}$  where  $C$  is the working capacity of the battery in amp hours (Ah) given a discharge rate of  $I$  (with  $n > 1$ ) measured in amps (A). The constant  $K > 0$  is the rated capacity of the battery.
- a. [5 points] Write a formula for the derivative of  $C$  at  $I = 3$  using the limit definition of the derivative. You do not need to evaluate or simplify this expression.
- b. [3 points] Is  $C$  increasing or decreasing at  $I = 3$ ? Justify your answer.
- c. [2 points] What is the concavity of the graph of  $C$  at  $I = 3$ ? Justify your answer.