

2. [10 points] Louis owns a small soda company and is experimenting with new flavors. Let  $b(p)$  model the number of thousands of bottles of bacon-flavored soda sold by his company per month if he charges  $p$  cents per bottle. You may assume  $b(p)$  is differentiable and invertible.

a. [2 points] Give a practical interpretation of the statement  $b^{-1}(8) = 150$ .

b. [3 points] Give a practical interpretation of the statement  $(b^{-1})'(4) = -10$ .

c. [3 points] Write an expression that is equal to the price (in cents) that the company would have to charge per bottle in order to sell twice as many bottles of bacon-flavored soda as it sells at a price of 125 cents per bottle.

d. [2 points] Which of the following is a correct formula for a function  $h(d)$  that gives the number of thousands of bottles sold per month at a price of  $d$  dollars per bottle? (Circle your answer.)

$$h(d) = 100b(d) \quad h(d) = \frac{b(d)}{100} \quad h(d) = b(100d) \quad h(d) = b\left(\frac{d}{100}\right)$$

3. [5 points] Use the limit definition of the derivative to write an explicit expression for  $r'(3)$  where  $r(t) = (t + 5)^{2t}$ . Do not simplify or evaluate the limit. Your answer should not include the letter  $r$ .

$$r'(3) = \underline{\hspace{10cm}}$$