7. [10 points] Let $N(u)=\left\{\begin{array}{ll}e+3^{u^{2}+k} & \text { if } u<1 \\ 5 e \ln (e+u-1) & \text { if } u \geq 1,\end{array}\right.$ where $k$ is a constant.
a. [6 points] Use the limit definition of the derivative to write an explicit expression for $N^{\prime}(-2)$. Your answer should not involve the letter $N$. Do not attempt to evaluate or simplify the limit. Please write your final answer in the answer box provided below.

Answer: $N^{\prime}(-2)=$ $\square$
b. [4 points] Find all values of $k$ so that $N(u)$ is continuous at $u=1$.

Show your work carefully, and leave your answer(s) in exact form.

Answer: $k=$ $\qquad$
8. [7 points] Suppose $w$ and $q$ are continuous and invertible functions.

The table below shows many values of $w$ and $q^{-1}$ (the inverse of $q$ ).

| $s$ | -4.7 | -3.3 | -1.8 | 0.7 | 1.1 | 1.6 | 2.1 | 2.5 | 4.1 | 5.2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $w(s)$ | 4.1 | 2.5 | 1.4 | 0 | -0.5 | -1.8 | -2 | -3.1 | -3.9 | -4.7 |
| $q^{-1}(s)$ | -3.7 | 0.1 | 0.7 | 2.5 | 4.1 | 5.1 | 5.2 | 7.3 | 9.5 | 11.3 |

a. [2 points] Find $q^{-1}(w(-4.7))$.
b. [2 points] Find $w(q(0.7))$.

Answer: $\qquad$ Answer:
c. [3 points] Find the average rate of change of $q(x)$ between $x=0.7$ and $x=5.2$. Be sure to show your work.

