

9. [9 points] Consider the rational function  $r$  defined by

$$r(x) = \frac{3(x - \sqrt{2})(\pi x + 7)^2(x + 1)}{(x + 1)(x - \sqrt{3})}.$$

For all of the following parts of this problem, leave your answers in *exact* form.

- a. [2 points] What is the domain of  $r(x)$ ?

**Answer:** \_\_\_\_\_

- b. [2 points] Find the *equations* of all vertical asymptotes of  $r(x)$ . If there are none, write NONE.

**Answer:** \_\_\_\_\_

- c. [2 points] Let  $p(x) = 3x^2 + 1.2x - 5$ . Find the *equations* of all horizontal asymptotes of  $\frac{r(x)}{p(x)}$ . If there are none, write NONE. Show your work or reasoning to justify your answer.

**Answer:** \_\_\_\_\_

- d. [3 points] If  $q(x) = \frac{2e^{kx}}{1 + 2^x}$ , find all values of  $k$  so that  $\lim_{x \rightarrow \infty} q(x) = 0$ . If there are none, write NONE. Show your work or reasoning to justify your answer.

**Answer:** \_\_\_\_\_