

8. [12 points] The size of the harvest at a kale farm is a function of the total amount of compost the farm uses in the fields.
- Let $K(c)$ be the size (as measured by weight) of the farm's kale harvest, in tons, when the farm uses c cubic meters (m^3) of compost.
 - Let $P(h)$ be the farm's profit, in thousands of dollars, when their kale harvest is h tons.

The functions $K(c)$ and $P(h)$ are differentiable, and the function $P(h)$ is invertible.

- a. [2 points] Using a complete sentence, give a practical interpretation of the equation

$$P^{-1}(86) = 53.$$

- b. [3 points] Write a single equation involving K , P , and/or P^{-1} that represents the following statement.

If the farm uses 1125 m^3 of compost, their profit will be twice as large as if they had used 700 m^3 of compost.

Answer: _____

- c. [3 points] Complete the following sentence to give a practical interpretation of the equation

$$K'(950) = 0.2.$$

If the farm uses 955 m^3 of compost instead of 950 m^3 , ...

- d. [4 points] Write a single equation involving the derivative function(s) K' , P' , and/or $(P^{-1})'$ that represents the following statement.

In order for the farm's profit to be \$101,500 rather than \$100,000, their kale harvest must be about 0.9 tons larger.

Answer: _____