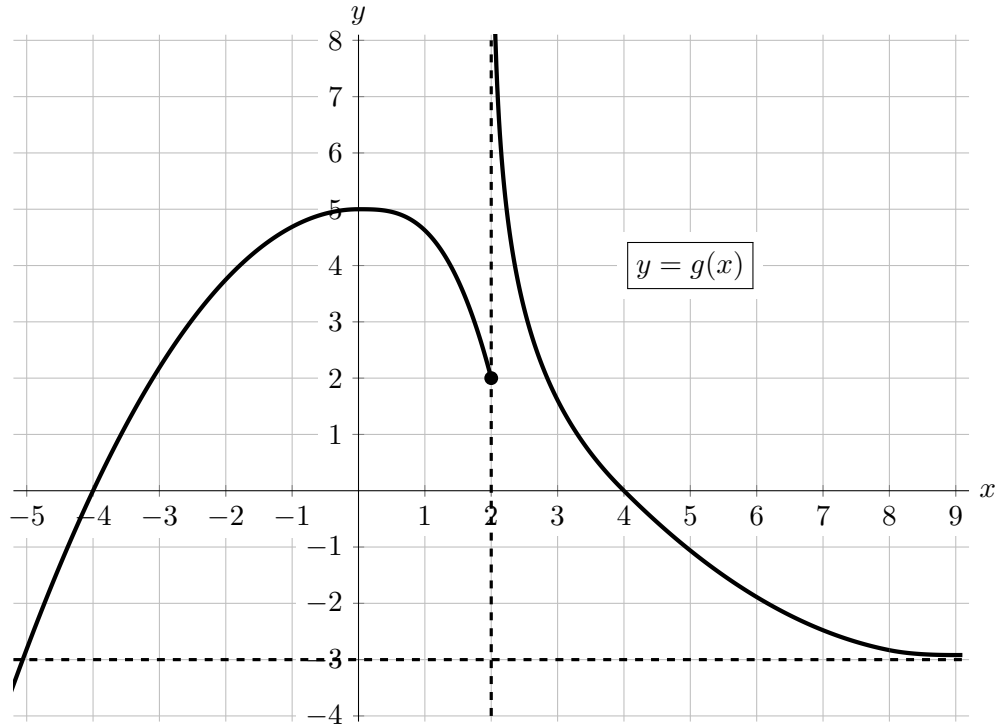


10. [9 points] A portion of the graph of a function  $g(x)$  is shown below.



The function  $g$  has the following characteristics.

- A vertical asymptote at  $x = 2$  (and no others).
- A horizontal asymptote at  $y = -3$  (and no others).
- $g(x)$  is continuous and increasing on the interval  $(-\infty, 0)$ .
- $g(x)$  is continuous and decreasing on the interval  $(2, \infty)$ .
- The tangent line to the graph of  $g(x)$  at  $x = 0$  is horizontal.

a. [5 points] Consider  $g'(x)$ , the derivative of  $g(x)$ .

Determine whether each statement below is TRUE or FALSE. Write out the entire word TRUE or FALSE as your answer. No explanation is required.

i.  $g'(-4) = 0$

ii.  $g'(0) = 0$

iii.  $g'(3) < g'(6)$

iv.  $g'(-4) = g'(4)$

v.  $g'(x)$  is decreasing on the interval  $(-2, 1)$

b. [4 points] Consider the function  $h(x) = 3g(x + 2)$ .

Determine whether each statement below is TRUE or FALSE. Write out the entire word TRUE or FALSE as your answer. No explanation is required.

i.  $h(x)$  is defined for all real numbers.

ii. The line  $y = -1$  is a horizontal asymptote of the graph of  $y = h(x)$ .

iii. The line  $x = 4$  is a vertical asymptote of the graph of  $y = h(x)$ .

iv.  $h(x)$  is not continuous at  $x = 0$ .