- **5**. [7 points]
  - a. [3 points] Let

$$Q(t) = 7 - \sin(t^2).$$

Suppose k is a nonzero constant. Write an explicit expression for the average rate of change of Q between t = 5 and t = 5 + k.

Your answer should not involve the letter Q. Do not attempt to simplify your expression.

Draw a box around your final answer.

**b**. [4 points] Let

$$P(w) = 6^{\arctan(4w)}$$
.

Use the limit definition of the derivative to write an explicit expression for P'(-3).

Your answer should not involve the letter P. Do not attempt to evaluate or simplify the limit.

Draw a box around your final answer.

- 6. [11 points] Define the following functions for an airplane taking off from a certain airport.
  - Let H(t) be the height above sea level, in kilometers (km), of the airplane t minutes after takeoff.
  - Let T(k) be the temperature of the air outside the airplane, in degrees Celsius (°C), at a height of k kilometers above sea level.

The functions H(t) and T(k) are differentiable and invertible.

- a. [2 points] Use a complete sentence to give a practical interpretation of the equation  $H^{-1}(6) = 5$ .
- **b.** [3 points] Write a single equation representing the following statement in terms of the functions H, T, and/or their inverses:

The temperature of the air outside the airplane fell by 12 °C in the first five minutes after takeoff.

c. [3 points] Complete the following sentence to give a practical interpretation of the equation

$$T'(9) = -10.$$

As the plane climbs from 8.8 km above sea level to 9 km above sea level...

- **d.** [3 points] Which of the following gives a valid interpretation of the equation  $(H^{-1})'(4) = 0.5$ ? Write down the Roman numeral corresponding to your choice. There is only one correct answer.
  - i. When the plane is at a height of 4 km, the temperature of the air outside the plane will decrease by about 0.5 degrees Celsius as the plane climbs an additional kilometer.
  - ii. It will take approximately 30 seconds for the airplane to climb from a height of 4 km to a height of 5 km.
  - iii. Four minutes into its flight, the plane will increase its height by about 0.5 km in the next minute.
  - iv. Once the plane has reached a height of 4 km, it will take about one minute to climb an additional 0.5 km.