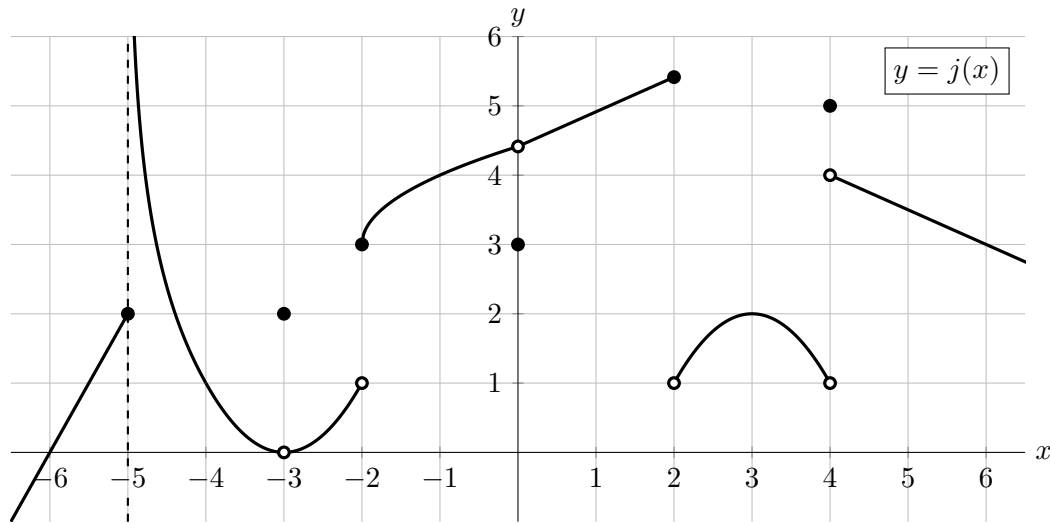


1. [11 points] Below is a portion of the graph of the function  $j(x)$ . Note that  $j(x)$  has a vertical asymptote at  $x = -5$ , and is linear on the intervals  $(-6, -5)$ ,  $(0, 2)$ , and  $(4, 6)$ .



- a. [1 point] At which of the following values of  $x$  is the function  $j(x)$  continuous? Circle all correct answers.

$x = -3$        $x = -2$        $x = 3$        $x = 4$       NONE OF THESE

- b. [6 points] Find the **exact** numerical value of each expression below, if possible. For any values that do not exist, including if they are limits that diverge to  $\pm\infty$ , write DNE.

i.  $\lim_{x \rightarrow 3} j(x) = \underline{\hspace{2cm}}$

iv.  $\lim_{x \rightarrow 0} \frac{j(5+x) - j(5)}{x} = \underline{\hspace{2cm}}$

ii.  $\lim_{x \rightarrow -3} j(x) = \underline{\hspace{2cm}}$

v.  $\lim_{x \rightarrow 2^+} j(x) = \underline{\hspace{2cm}}$

iii.  $\lim_{x \rightarrow 4} j(x) = \underline{\hspace{2cm}}$

vi.  $\lim_{x \rightarrow -5^+} \frac{1}{j(x)} = \underline{\hspace{2cm}}$

- c. [2 points] Consider the function  $k(x) = 2 \cdot j\left(\frac{1}{2}(x - 9)\right) + 1$ . Which of the following must be a vertical asymptote of  $k(x)$ ? Circle the one correct answer.

$x = -9$        $x = -5$        $x = -3$        $x = -1$        $x = 1$

- d. [2 points] Given that  $j'(-4) = -2$ , find an equation of the line tangent to the graph of  $j(x)$  at the point  $(-4, 1)$ .

**Answer:** \_\_\_\_\_