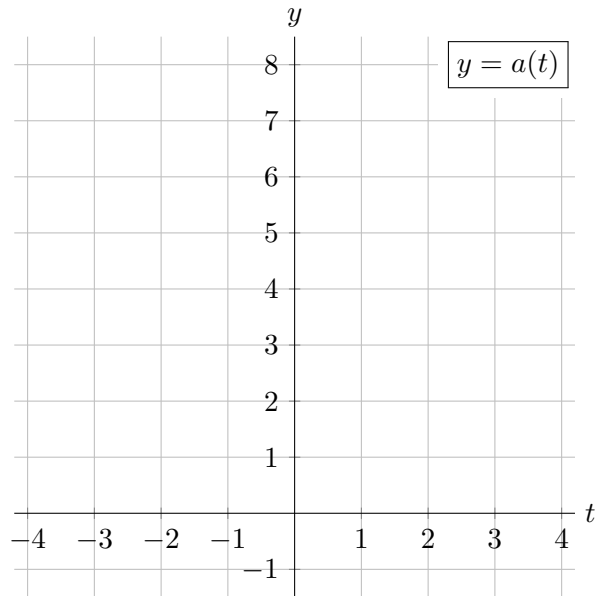


7. [5 points] Suppose  $a(t)$  is the altitude in hundreds of meters above sea level of a certain hot air balloon  $t$  hours after 12pm noon on a sunny day. Carefully draw a plausible graph of  $a(t)$  on the given axes, assuming the following are true:

- the balloon lifts off the ground at 8am from a point that is 100 meters above sea level, and stays in the air until it lands at the same location at 4pm;
- the rate at which the balloon's altitude is changing is constant between 9am and 10am, and again between 2pm and 4pm;
- at 9:30am, the balloon is **ascending** twice as fast as it is **descending** at 3pm;
- the balloon spends at least one full hour at its maximum altitude of 700 meters.



8. [6 points] Let  $g(x)$  be the piecewise function defined by

$$g(x) = \begin{cases} \frac{-4(x+1)}{(x^2-1)(x+4)} & x < 0 \\ e^{A(x-1)} + \frac{B(x+1)^2(x-2)}{2(x-3)(x-2)^2} & x \geq 0 \end{cases}$$

where  $A$  and  $B$  are nonzero constants.

- a. [3 points] List the  $x$ -coordinates of all **vertical asymptotes** of  $g(x)$ .

**Answer:**  $x =$  \_\_\_\_\_

- b. [3 points] Find values of the constants  $A$  and  $B$  such that  $g(x)$  is continuous at  $x = 0$  and  $g(x)$  has a **horizontal asymptote** at  $y = -3$ .

**Answers:**  $A =$  \_\_\_\_\_  $B =$  \_\_\_\_\_