4. (6 points) A circus is planning to visit your hometown. They claim to have a mummy that is 15,000 years old, but the citizens of your town are suspicious. The town council is given a sample of the mummy for a carbon-14 analysis. Your old high school science teacher is able to find that $33 \%$ of the mummy's carbon-14 remains. Using the fact that the half-life of carbon-14 is 5,730 years, determine the age of the mummy that the circus is bringing to town. [Show your work!]

We know that since the carbon-14 decays exponentially, that the formula for the amount of carbon-14 left after $t$ years is given by

$$
P=P_{0} e^{r t}
$$

where $P_{0}$ is the initial amount and $r$ is the exponential rate of decay.
To find $r$, we use that the half-life of carbon-14 is 5730 years. So we have

$$
\begin{aligned}
\frac{1}{2} P_{0} & =P_{0} e^{5730 r} \\
\frac{1}{2} & =e^{5730 r} \\
-\ln (2) & =5730 r \\
r & =\frac{-\ln (2)}{5730} .
\end{aligned}
$$

So now we can find the time elapsed when $33 \%$ of the mummy's carbon remains.

$$
\begin{aligned}
0.33 P_{0} & =P_{0} e^{\frac{-\ln (2) t}{5730}} \\
\ln (0.33) & =\frac{-\ln (2) t}{5730} \\
t & =9,164.92 \text { years }
\end{aligned}
$$

Therefore, the circus is exaggerating the age of their mummy.
5. (3 points each) The marketing department of Lay's Potato Chips decides to do a study on the number of chips a person craves as a function of the number of chips already eaten by that person. Their function turns out to be the rational function

$$
C(x)=\frac{2 x^{2}}{(x-1)^{2}},
$$

where $C(x)$ is the number of additional chips a person who has eaten $x$ chips is still craving to eat.
(a) How is Lay's famous slogan "You can't eat just one" summarized by this equation?

The slogan is given by the fact that 1 is not in the domain of $C(x)$. This shows that it is impossible to eat one Lay's potato chip.
(b) What is the horizontal asymptote of $C(x)$ ? What does this say about a person with an unlimited supply of chips who can't control his/her cravings?

The horizontal asymptote is at $y=2$. This says that in the long run a person will always crave 2 more Lay's potato chips. So if one could not control one's cravings, one would eat potato chips forever.

