

5. (2 points each) Circle “TRUE” or “FALSE” for each of the following problems. Circle “TRUE” only if the statement is *always* true. No explanation is necessary.

- (a) If  $g(x)$  is an everywhere differentiable function, then so is  $f(x) = ag(x - h) + b$ , where  $a$ ,  $b$  and  $h$  are constants.

TRUE      FALSE

- (b) Suppose  $H(t)$  and  $T(t)$  are differentiable functions, and  $T(t) = H(t) - 4$ . Then  $H$  and  $T$  have the same derivative at each  $t$ .

TRUE      FALSE

- (c) If  $l$  and  $m$  are inverse functions and the graph of  $m$  crosses the line  $y = x$ , the graph of  $l$  must also cross this line at the same point.

TRUE      FALSE

- (d) If  $b$  is a positive constant, then  $\lim_{h \rightarrow 0} \frac{\sqrt{b+h} - \sqrt{b}}{h} = 0.5 b^{-1/2}$ .

TRUE      FALSE

- (e) If  $s(t)$  gives the position of an object moving at a constant velocity, then the object’s instantaneous velocity at  $t = a$  is equal to  $\frac{s(b) - s(a)}{b - a}$  for all  $a \neq b$ .

TRUE      FALSE

- (f) If  $t$  is a differentiable concave up function, then  $t'(a) < \frac{t(b) - t(a)}{b - a}$  for all  $a < b$ .

TRUE      FALSE

- (g) For any constant  $a$ , the equation  $ax = e^{2 \ln x} + a^2$  has exactly one solution.

TRUE      FALSE