8. (15 points) The functions r = f(t) and V = g(r) give the radius and the volume of a commercial hot air balloon that is being inflated for testing. The variables t and r are measured in minutes and feet respectively, while the volume V is measured in cubic feet. The inflation begins at t = 0.

In each case, translate the words or phrases given below into the precise mathematical expression that represents them. This mathematical expression will consist *only* of numbers, variables and symbols defined in this problem, and other mathematical symbols related to function notation and operations. For example, in problem 1(b) the notation "p'(6)" is a mathematical expression. There we gave an expression and you were asked to interpret. Here we are giving the interpretation and you are to supply the mathematical expression.

You may assume V and r are strictly increasing, differentiable functions.

(a) The average rate of change in the volume of the balloon when the radius expands from 10 to 12 feet:

Mathematical Expression _____

(b) The volume of the balloon t minutes after inflation began:

Mathematical	Expression

(c) The volume of the balloon if the radius was twice as big:

Mathematical Expression

(d) The time elapsed when the radius of the balloon is 30 feet:

Mathematical	Expression	

(e) The time elapsed when the volume of the balloon is 10,000 cubic feet:

Mathematical Expression