

8. A continuous function f , defined for all x , is always decreasing and concave up. Suppose $f(6) = -6$ and $f'(6) = -1.5$.

(a) (2 points) How many zeros does f have? Justify your answer.

(b) (2 points) Can $f'(2) = -1$? Justify your answer.

(c) (4 points) Circle all intervals below in which f has at least one zero. Justify your choices with a picture and a short description.

- i. $(-\infty, -6)$
- ii. $[-6, -2)$
- iii. $[-2, -1)$
- iv. $[-1, 1)$
- v. $[1, 2)$
- vi. $[2, 6)$
- vii. $[6, \infty)$