

9. (12 points) On the axes below, sketch a function  $f$  satisfying all the following properties. Be careful to label all important points on the axes.

- $f$  has a vertical asymptote at  $x = 4$
- $f$  is continuous on  $(-\infty, 4)$  and on  $(4, \infty)$
- $f'(x) > 0$  and  $f''(x) > 0$  for all  $x$  in  $(-\infty, 0)$
- $f(0) = 2$
- $f$  is not differentiable at  $x = 0$
- $f''(x) > 0$  for all  $x$  in  $(0, 2)$
- $f'(2) > 0$
- $f''(x) < 0$  for all  $x$  in  $(2, 4)$
- For all  $x > 4$ ,  $f$  is decreasing and is concave up
- $\lim_{x \rightarrow \infty} f(x) = 1$

One possible solution is shown below.

