8. [10 points] The graphs of two functions $f$ and $g$ are shown below, along with a table of values for a function $h$.



| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $h(x)$ | 15 | 2 | -5 | -6 | -1 | 10 | 27 |

a. [4 points] Compute each of the following.

- $h(g(1))=$ $\qquad$

Solution: $h(g(1))=h(0)=-6$

- $f(1+h(1))=$ $\qquad$

Solution: $f(1+h(1))=f(1+(-1))=f(0)=0$
b. [3 points] There exists a number $B$ so that $f^{\prime}(x)=g(x+B)$. Find $B$.

Solution: Since $f$ is flat at $x=-2, x=0$, and $x=1$, we know $f^{\prime}$ has zeroes at these spots. Since $g$ has zeroes at $x=1, x=3$, and $x=4$, we need to shift $g$ to the left by 3 to get $f^{\prime}$. Thus, $B=3$.
c. [3 points] Is it possible that $f^{\prime \prime}=h$ ? Briefly justify your answer.

Solution: No. At $x=1, f$ is concave up, so $f^{\prime \prime}(1) \geq 0$, but $h(1)=-1$.

