2. [13 points] Below is a table of values for an invertible, differentiable function $f(x)$ and the graph of a function $g(x)$. Use these to answer the following questions:

| $x$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 8 | 7 | 3 | 2 | 1.5 | 1 |


a. [1 point] Give one number in the interval $[-5,5]$ that is not in the domain of $g$.

Solution: 3
b. [1 point] Give one number in the interval $[-5,5]$ that is not in the domain of $g^{-1}$.

Solution: Anything in $(-4,-1] \cup\{4\}$. For example, 4.
c. [8 points] Evaluate the following:
(i) $f(f(5))$

Solution: $\quad f(f(5))=f(1)=7$.
(ii) $g^{-1}\left(f^{-1}(2)\right)$

Solution: $\quad g^{-1}\left(f^{-1}(2)\right)=g^{-1}(3)=1$.
(iii) $\lim _{x \rightarrow 3} g(x)$

Solution: 4, found from graph of $g$.
(iv) $g^{\prime}(1+f(2))$

Solution: $\quad g^{\prime}(1+f(2))=g^{\prime}(4)=\frac{1}{2}$ looking at the slope on the graph of $g$ at $x=4$.
d. [3 points] Approximate $f^{\prime}(3)$. (Be sure to show your work.)

Solution: Acceptable answers: $-1,-\frac{1}{2},-\frac{3}{4}$. Found approximating the derivative via a difference quotient.

