

1. [11 points] The table below gives several values of a continuous, invertible function  $f(x)$ . Assume that the domain of both  $f(x)$  and  $f'(x)$  is the interval  $(-\infty, \infty)$ .

$x$	0	3	6	9	12	15	18	21	24
$f(x)$	-7	-3.5	-2	3	4.5	6	7	9	19

- a. [3 points] Evaluate each of the following.

(i)  $f(f(15))$

**Answer:**  $f(f(15)) =$  \_\_\_\_\_

(ii)  $f^{-1}(3)$

**Answer:**  $f^{-1}(3) =$  \_\_\_\_\_

(iii)  $f^{-1}(2f(12))$

**Answer:**  $f^{-1}(2f(12)) =$  \_\_\_\_\_

- b. [2 points] Compute the average rate of change of  $f$  on the interval  $3 \leq x \leq 18$ .

**Answer:** \_\_\_\_\_

- c. [2 points] Estimate  $f'(19)$ .

**Answer:**  $f'(19) \approx$  \_\_\_\_\_

- d. [2 points] Let  $g(x) = f^{-1}(x)$ . Estimate  $g'(5)$ .

**Answer:**  $g'(5) \approx$  \_\_\_\_\_

- e. [2 points] Suppose  $f'(0) = 2$ . Find an equation for the tangent line to the graph of  $y = f(x)$  at  $x = 0$ .

**Answer:** \_\_\_\_\_