

1. [8 points] The table below gives several values of the continuous, invertible, differentiable functions  $f(x)$  and  $g(x)$ .

$x$	1.8	1.9	2	2.1	2.2	2.3
$f(x)$	2.5	2.35	2.2	2	1.8	1.7
$g(x)$	1.6	1.75	1.8	1.9	2	2.2

- a. [2 points] Compute  $f(g^{-1}(2))$ .

**Answer:**  $f(g^{-1}(2)) =$  \_\_\_\_\_

- b. [2 points] Estimate  $f'(2)$ .

**Answer:**  $f'(2) \approx$  \_\_\_\_\_

- c. [2 points] Let  $j(x) = g^{-1}(x)$ . Estimate  $j'(1.9)$ .

**Answer:**  $j'(1.9) \approx$  \_\_\_\_\_

- d. [2 points] Suppose  $p(x)$  is a function whose derivative is given by  $p'(x) = \ln(x^3 + 11)$ . Compute  $p'(f(2))$ .

**Answer:**  $p'(f(2)) =$  \_\_\_\_\_

2. [6 points] Suppose  $a$  and  $b$  are constants with  $a > 3$  and  $b > 0$ , and let  $h(t) = a^{-bt}$ .

- a. [3 points] Find constants  $P_0$  and  $k$  so that  $h(t) = P_0 e^{kt}$ . (Your answers may involve the constants  $a$  and/or  $b$ .)

**Answer:**  $P_0 =$  \_\_\_\_\_ and  $k =$  \_\_\_\_\_

- b. [3 points] Circle all the statements below that must be true about the function  $h(t)$ . If none of the statements must be true, circle NONE OF THESE.

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|---|---|
| i. The domain of $h(t)$ is the interval $(-\infty, \infty)$ . | v. $t = 0$ is a vertical asymptote of the graph of $h(t)$ . |
| ii. The range of $h(t)$ is the interval $(-\infty, \infty)$ . | vi. $\lim_{t \rightarrow \infty} h(t) = 0$ .                |
| iii. $h(t)$ is an increasing function on its domain.          | vii. $\lim_{t \rightarrow -\infty} h(t) = 0$ .              |
| iv. $h(t)$ is concave up on its domain.                       | NONE OF THESE   |