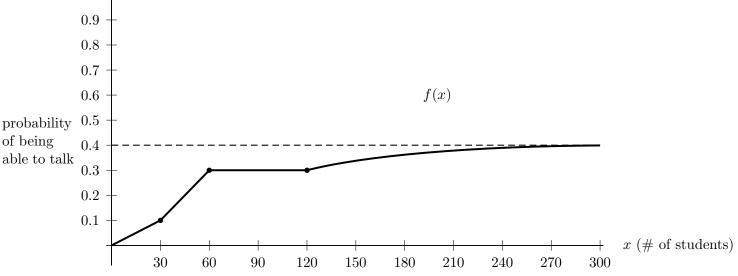
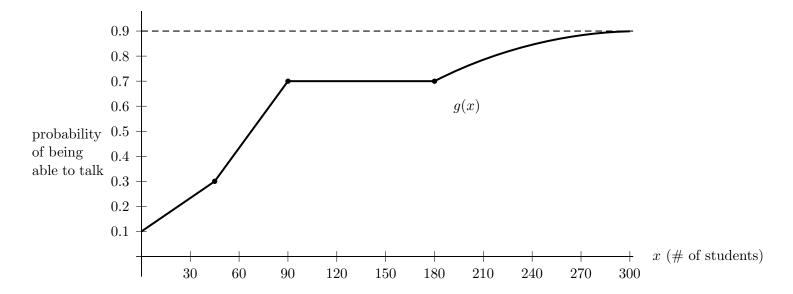
9. [12 points] Lauren has just been approached by a talking kangaroo named Skipper. Lauren is alarmed by Skipper's ability to talk so she asks him if all kangaroos can talk. Skipper tells her that a kangaroo's probability of being able to talk depends on how much attention they receive from University of Sydney students. He also explains that this relationship has changed recently. Let f(x) be the probability that a kangaroo born prior to 5 weeks ago is able to talk if x students have paid attention to that kangaroo in their life. Below is a graph of the function f(x).



**a.** [4 points] Let g(x) be the probability that a kangaroo born within the last 5 weeks is able to talk if x students have paid attention to that kangaroo in their life. A graph of g(x) is given below.



It turns out that for  $x \ge 0$ , g(x) can be expressed as a transformation of f(x). Write a formula for g(x) as a transformation of f(x).

Answer:

Problem continues on the next page.

This is a continuation of the problem from the previous page.

**b.** [3 points] Let h(y) be the number of students that pay attention to a kangaroo over the duration of the kangaroo's life if the kangaroo has y docile units. (Note that we measure docileness in terms of docile units.) Give a practical interpretation of g(h(5)).

c. [3 points] The number of students who pay attention to a kangaroo with y docile units is proportional to  $y^2$ . Find a formula for h(y) if a total of 160 students pay attention to a kangaroo with 4 docile units during its life.

Answer: h(y) =

**d**. [2 points] Calculate f(h(3)).