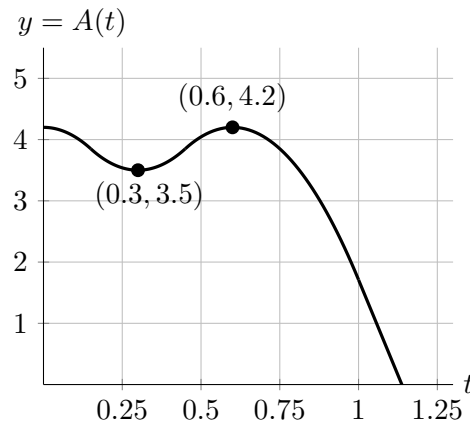


3. [13 points] Tom organizes another meeting of his Science Club, but this time only Anne and John can make it. The meeting is at 2 pm, so they both start walking from their houses to Tom's at 1 pm. At 1:18 pm, Anne realizes she forgot her wallet, so she goes back home to get it before heading over to Tom's house.

Anne's distance in kilometers,  $A(t)$ , and John's distance in kilometers,  $J(t)$ , to Tom's house  $t$  hours after 1 pm are given by the graph and the table below. Assume that both of them walk along a straight line.

$t$	0	0.2	0.4	0.5	0.8	0.9
$J(t)$	5.5	4.3	3.2	2.8	0.8	0



- a. [1 point] How many kilometers from Tom's house is Anne's house?

*Solution:* 4.2 km.

- b. [2 points] Estimate  $J'(0.4)$ . Show all your computations. Include units.

*Solution:*  $J'(0.4) \approx \frac{2.8 - 3.2}{0.5 - 0.4} = -\frac{0.4}{0.1} = -4$  kilometers per hour.

- c. [3 points] Rank John's average velocity over the time intervals

(I)  $0.2 \leq t \leq 0.4$

(II)  $0.5 \leq t \leq 0.9$

(III)  $0.8 \leq t \leq 0.9$

from least to greatest. Show your work and indicate your final answer by filling in the blanks with I, II, III.

*Solution:*  $[0.2, 0.4]: \frac{3.2 - 4.3}{0.2} = -5.5$ ,  $[0.5, 0.9]: \frac{0 - 2.8}{0.4} = -7$ ,  
 $[0.8, 0.9]: \frac{0 - 0.8}{0.1} = -8$  III  $\leq$  II  $\leq$  I.

- d. [2 points] What was the total distance travelled by Anne?

*Solution:* distance =  $2(0.7) + 4.2 = 5.6$  kilometers.

- e. [2 points] At which of the following times was Anne's speed the largest? Circle the correct answer(s).

*Solution:*

$t = 0.05$

$t = 0.3$

$t = 0.4$

$t = 0.6$

$t = 1$

- f. [3 points] On which of the following intervals is  $A(t)$  invertible? Circle the correct answer(s).

*Solution:*

$[0, 0.6]$

$[0.3, 0.6]$

$[0.1, 0.5]$

$[0.6, 1]$

$[0, 1]$