

3. (12 points) This table describes two functions,  $f(x)$  and  $g(x)$ .

$x$	$f(x)$	$f'(x)$	$g(x)$	$g'(x)$
1	$\pi$	1.4	1.5	-0.2
3	5	1	1	3
5	$2.5\pi$	0.3	6	4

a) (4 pts) Find  $h'(3)$ , assuming  $h(x) = f(g(x))$ . Show your work.

$$\begin{aligned} h'(3) &= f'(g(3)) \cdot g'(3), \text{ by the Chain Rule.} \\ &= f'(1) \cdot g'(3) \\ &= (1.4) \cdot (3) = 4.2 \end{aligned}$$

b) (4 pts) Find  $j'(5)$ , if  $j(x) = \frac{f(x)}{g(x)}$ . Show your work.

$$\begin{aligned} j'(5) &= \frac{g(5) f'(5) - f(5) g'(5)}{g(5)^2} \quad \text{by the Quotient Rule} \\ &= \frac{6 \cdot (0.3) - (2.5\pi) 4}{36} = \frac{1.8 - 10\pi}{36} \end{aligned}$$

c) (4 pts) Find  $k'(5)$ , where  $k(x) = xg(x)$ . Show your work.

$$\begin{aligned} k'(x) &= 1 \cdot g(x) + x \cdot g'(x), \text{ by the Product Rule,} \\ k'(5) &= 1 \cdot 6 + 5 \cdot 4 = 26 \end{aligned}$$