

4. (12 points) Ellen and Renzo ran the Detroit marathon last weekend. The distance Ellen traveled (in meters) is given by  $E(t)$  where  $t$  is time measured in seconds since the start of the race. Similarly, the distance in meters Renzo traveled is given by the function  $R(t)$ . For  $x$  measured in meters let  $F(x) = R(E^{-1}(x))$ . Assume that Ellen moves forward throughout the race—she does not even take a rest!

(a) What is the practical interpretation of  $F(50)$ .

- (b) After the initial blast of speed from her start, Ellen ran at a constant rate of 5 meters per second for  $2 < t < 10$ , and she had run a distance of 39 meters after 7 seconds. Renzo wore a device that tracked the distance he had run at one second intervals. The data he collected is summarized in the table below.

$t$	0	1	2	3	4	5	6	7	8	9	10
$R(t)$	0	10	16	22	28	34	40	46	52	58	64

Use any of the information above to approximate  $F'(39)$ .

- (c) Give a practical interpretation of  $F'(39)$ .