

3. (14 points) Find the values of the constants a , b and c such that the function

$$f(x) = ax^2 + bx + c$$

“fits” the function

$$g(x) = -2\ln(x + 1) + 0.5e^x + 1.5\sin(x)$$

near $x = 0$ in the sense that:

$$g(0) = f(0), \quad g'(0) = f'(0) \quad \text{and} \quad g''(0) = f''(0).$$

Show all work.

$$a = \underline{\hspace{4cm}}$$

$$b = \underline{\hspace{4cm}}$$

$$c = \underline{\hspace{4cm}}$$