

1. For the following questions select true if the statement is *always* true, and false otherwise. Each question is worth 1 point.

(a) If  $f$  is differentiable and  $f'(p) = 0$  or  $f'(p)$  is undefined, then  $f(p)$  is either a local maximum or a local minimum.

True

False

(b) For  $f$  a twice differentiable function, if  $f'$  is increasing, then  $f$  is concave up and increasing.

True

False

(c) The global maximum of  $f(x) = x^2$  on every closed interval is at one of the endpoints of the interval.

True

False

(d) If  $f(x)$  has an inverse function  $g(x)$ , then  $g'(x) = 1/f'(x)$ .

True

False

(e) If a function is periodic with period  $c$ , then so is its derivative.

True

False

(f) If  $C(q)$  represents the cost of producing a quantity  $q$  of goods, then  $C'(0)$  represents the fixed costs.

True

False

(g) If a differentiable function  $f(x)$  has a global maximum on the interval  $0 \leq x \leq 10$  at  $x = 0$ , then  $f'(x) \leq 0$  for  $0 \leq x \leq 10$ .

True

False

(h) If  $f(x)$  is differentiable and concave up, then  $f'(a) < \frac{f(b)-f(a)}{b-a}$  for  $a < b$ .

True

False

(i) If you zoom in with your calculator on the graph of  $y = f(x)$  in a small interval around  $x = 10$  and see a straight line, then the slope of that line equals the derivative  $f'(10)$ .

True

False

(j) If  $f'(x) \geq 0$  for all  $x$ , then  $f(a) \leq f(b)$  whenever  $a \leq b$ .

True

False