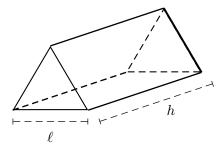
3. [12 points] Consider the prism with equilateral triangles of side length  $\ell$  centimeters for ends and a length of h centimeters, illustrated below. The volume of this prism is  $\sqrt{3} \ell^2 h/4$ . You may find it useful to note that the area of an equilateral triangle of side length  $\ell$  is  $\sqrt{3} \ell^2/4$ .



a. [4 points] Give the equation of the surface area of this prism, listing units.

Surface area=\_\_\_\_

**b.** [8 points] If the prism has a fixed volume of 16 cm<sup>3</sup>, find the values of  $\ell$  and h which minimize the surface area. Clearly justify that you have found the minimum.