

5. [14 points] The function  $f$  has a continuous second derivative on the interval  $10 \leq x \leq 19$ . Some values of its derivative function  $f'$  are given in the table below.

$x$	10	11	12	13	14	15	16	17	18	19
$f'(x)$	-34	-3	-1	-2	-3	31	62	70	66	37

- a. [4 points]  $f$  has exactly one inflection point on the interval  $15 \leq x \leq 19$ . Given the information provided, give the smallest  $x$  interval on which this inflection point is guaranteed to lie, making it clear whether your endpoints are included.

- b. [8 points]  $f$  has exactly four critical points, with  $x$ -values 11.2, 11.7, 12.6, and 14.2, respectively. Classify each point as a local minimum, a local maximum, or neither, given that  $f$  has either a local maximum or a local minimum at  $x = 11.2$ . For each point below, circle only one option.

At  $x = 11.2$ ,  $f$  has            **a local maximum**            **a local minimum**

At  $x = 11.7$ ,  $f$  has            **a local maximum**            **a local minimum**            **neither**

At  $x = 12.6$ ,  $f$  has            **a local maximum**            **a local minimum**            **neither**

At  $x = 14.2$ ,  $f$  has            **a local maximum**            **a local minimum**            **neither**

- c. [2 points] Is there at least one inflection point on the interval  $11 < x < 12$ ? (Circle one.)

**Yes**

**No**

**Not possible to determine**