7. [13 points] Consider the family of functions

$$
y=a x^{b} \ln x
$$

where $a$ and $b$ are nonzero constants.
a. [4 points] Calculate $\frac{d y}{d x}$ in terms of the constants $a$ and $b$.
b. [9 points] Find specific values of $a$ and $b$ so that the resulting function has a local maximum at the point $(e, 1)$. You must show that $(e, 1)$ is a local maximum to receive full credit.

