5. [12 points] In Srebmun Foyoj, Maddy and Cal are eating lava cake. Let $T(v)$ be the time (in seconds) it takes Maddy to eat a $v \mathrm{~cm}^{3}$ serving of lava cake. Assume $T(v)$ is invertible and differentiable for $0<v<1000$. Several values of $T(v)$ and its first and second derivatives are given in the table below.

| $v$ | 10 | 15 | 60 | 100 | 150 | 200 | 300 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T(v)$ | 11 | 22 | 84 | 194 | 393 | 513 | 912 |
| $T^{\prime}(v)$ | 2.4 | 1.9 | 1.8 | 3.6 | 3.7 | 0.9 | 17.5 |
| $T^{\prime \prime}(v)$ | -0.11 | -0.08 | 0.05 | 0.04 | -0.04 | -0.05 | 0.59 |

Remember to show your work carefully.
a. [4 points] Use an appropriate linear approximation to estimate the amount of time it takes Maddy to eat a $64 \mathrm{~cm}^{3}$ serving of lava cake. Include units.


#### Abstract

Answer: b. [4 points] Use the quadratic approximation of $T(v)$ at $v=200$ to estimate $T(205)$. (Recall that a formula for the quadratic approximation $Q(x)$ of a function $f(x)$ at $x=a$ is $Q(x)=f(a)+f^{\prime}(a)(x-a)+\frac{f^{\prime \prime}(a)}{2}(x-a)^{2}$.


Answer: $T(205) \approx$ $\qquad$
c. [4 points] Let $C(v)$ be the time (in seconds) it takes Cal to eat a $v \mathrm{~cm}^{3}$ serving of lava cake, and suppose $C(v)=T(\sqrt{v})$. Let $L(v)$ be the local linearization of $C(v)$ at $v=100$. Find a formula for $L(v)$. Your answer should not include the function names $T$ or $C$.
$\qquad$

