## **9**. [14 points]

- **a.** [8 points] Consider functions f satisfying <u>all</u> of the following conditions:
  - f(x) is differentiable on the interval 0 < x < 8.
  - The critical points of f(x) in the interval 0 < x < 8 are x = 2, 4, and 6. (f(x)) has no other critical points in this interval.)
  - The table below shows some values of f(x) and of its derivative f'(x).

For each of the statements below, decide whether the statement is true for ALL functions f satisfying all of the conditions described above, for SOME of these functions f, or for NONE of these functions f. Circle the <u>one</u> correct choice for each statement.

(i) f(x) has a local minimum at x = 2.

ALL SOME NONE

(ii) f'(3) > 0.

ALL SOME NONE

(iii) f(x) has a local maximum at x = 4.

ALL SOME NONE

(iv) There is exactly one value of a with 3 < a < 7 such that f(x) has a local maximum at x = a.

ALL SOME NONE

**b.** [6 points] Consider functions g satisfying all of the following conditions:

- g(z) and g'(z) are differentiable on the interval 12 < z < 18.
- The critical points of g(z) in the interval 12 < z < 18 are z = 14 and z = 16. (g(z) has no other critical points in this interval.)
- The table below shows some values of g(z) and of its second derivative g''(z).

For each of the statements below, decide whether the statement is true for ALL functions g satisfying all of the conditions described above, for SOME of these functions g, or for NONE of these functions g. Circle the <u>one</u> correct choice for each statement.

(i) q(z) has a local extremum at z = 14.

ALL SOME NONE

(ii) g'(15) > 0.

ALL SOME NONE

(iii) g(z) has an inflection point at z = 16.

ALL SOME NONE