9. [14 points]
a. [8 points] Consider functions $f$ satisfying all of the following conditions:

- $f(x)$ is differentiable on the interval $0<x<8$.
- The critical points of $f(x)$ in the interval $0<x<8$ are $x=2$, 4, and 6. ( $f(x)$ has no other critical points in this interval.)
- The table below shows some values of $f(x)$ and of its derivative $f^{\prime}(x)$.

| $x$ | 1 | 3 | 5 | 7 |
| :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 3 | 6 | 11 | 0 |
| $f^{\prime}(x)$ | -1 | $?$ | $?$ | -1 |

For each of the statements below, decide whether the statement is true for all functions $f$ satisfying all of the conditions described above, for SOME of these functions $f$, or for NONE of these functions $f$. Circle the one correct choice for each statement.
(i) $\quad f(x)$ has a local minimum at $x=2$.
ALL
SOME
NONE
(ii) $f^{\prime}(3)>0$.

ALL SOME NONE
(iii) $f(x)$ has a local maximum at $x=4$.

ALL SOME NONE
(iv) There is exactly one value of $a$ with $3<a<7$ such that $f(x)$ has a local maximum at $x=a$.

ALL
SOME
NONE
b. [6 points] Consider functions $g$ satisfying all of the following conditions:

- $g(z)$ and $g^{\prime}(z)$ are differentiable on the interval $12<z<18$.
- The critical points of $g(z)$ in the interval $12<z<18$ are $z=14$ and $z=16 .(g(z)$ has no other critical points in this interval.)
- The table below shows some values of $g(z)$ and of its second derivative $g^{\prime \prime}(z)$.

| $z$ | 13 | 14 | 15 | 16 | 17 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $g(z)$ | 8 | $?$ | 6 | $?$ | 2 |
| $g^{\prime \prime}(z)$ | $?$ | -1 | $?$ | 0 | $?$ |

For each of the statements below, decide whether the statement is true for all functions $g$ satisfying all of the conditions described above, for sOME of these functions $g$, or for NONE of these functions $g$. Circle the one correct choice for each statement.
(i) $g(z)$ has a local extremum at $z=14$.
ALL
SOME
NONE
(ii) $g^{\prime}(15)>0$.

ALL
SOME
NONE
(iii) $g(z)$ has an inflection point at $z=16$.

