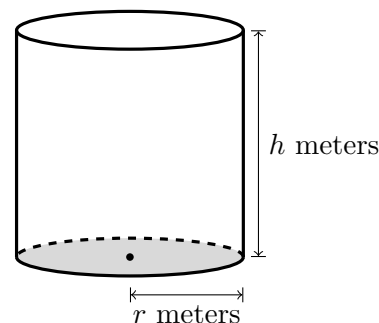


2. [10 points] Suma is making cylindrical paper cups that will be used to serve milkshakes at Qabil's Creamery. She rolls paper into a cylinder and then attaches it to the base. The thicker material that she uses for the base costs \$4.30 per square meter, and the lighter material that she uses for the vertical part of the cup costs \$2.20 per square meter. The radius of the circular base is  $r$  meters, and the height of the cup is  $h$  meters, as shown in the diagram on the right. It may be helpful to know that the surface area of the vertical portion of the cup is  $2\pi rh$ .



*Note:* The top of the cup is left open.

Throughout this problem, assume that the material that Suma uses to make one paper cup costs \$0.12.

- a. [4 points] Find a formula for  $h$  in terms of  $r$ .

**Answer:**  $h =$  \_\_\_\_\_

- b. [2 points] Let  $V(r)$  be the volume (in cubic meters) of the cup that Suma makes given that the material for the cup costs \$0.12 and the radius of the cup is  $r$  meters. Find a formula for  $V(r)$ . The variable  $h$  should not appear in your answer. (Note: This is the function that Suma would use to find the value of  $r$  maximizing the volume of the cup, but you should not do the optimization in this case.)

**Answer:**  $V(r) =$  \_\_\_\_\_

- c. [4 points] In the context of this problem, what is the domain of  $V(r)$ ?

**Answer:** \_\_\_\_\_