5. [9 points] In each of the following questions, draw a graph satisfying all the properties listed. There may be many correct answers. Make sure that your graph clearly shows all of the properties listed.
a. [5 points] The function $f(x)$ satisfies each of the following properties:

- $f(x)$ is continuous on $(0,8)$.
- $f(x)$ has a local maximum at $x=5$.
- $f^{\prime \prime}(x)<0$ on $(4,7)$.
- $\lim _{x \rightarrow 2^{-}} f^{\prime}(x)=\infty$ and
$\lim _{x \rightarrow 2^{+}} f^{\prime}(x)=0$

b. [4 points] The function $g(x)$ satisfies each of the following properties:
- $g(x)$ is defined on $(0,8)$.
- $g(x)$ has an inflection point at $x=3$.
- $g(x)$ is discontinuous at $x=6$.
- $g(x)$ has a local maximum at $x=6$.
- $g(x)$ has global maxima only at $x=1$ and $x=5$.


